Reasoning about a Highly Connected World

Book by David Easley and Jon Kleinberg

- I. Graph Theory and Social Networks
- II. Game Theory
- III. Markets and Strategic Interaction in Networks
- IV. Information Networks and the World Wide Web
- V. Network Dynamics: Population Models
- VI. Network Dynamics: Structural Models
- VII. Institutions and Aggregate Behavior

#### Outline

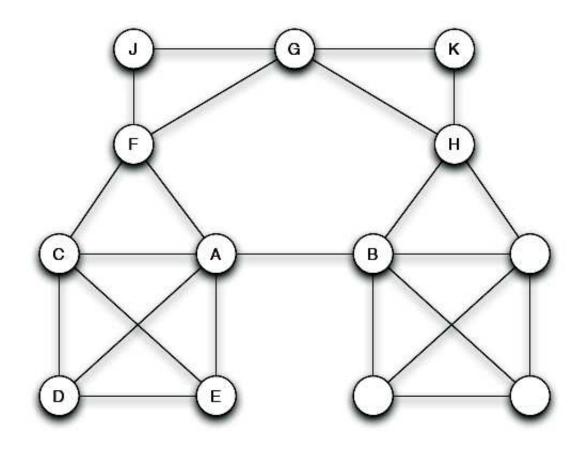
#### I. Graph Theory and Social Networks

- Graphs
- □ Strong and Weak Ties
- Networks in Their Surrounding Contexts
- Positive and Negative Relationships

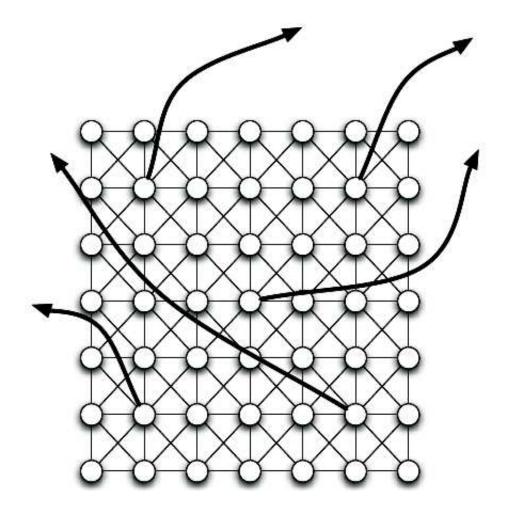
#### II. Game Theory

- III. Markets and Strategic Interaction in Networks
- IV. Information Networks and the World Wide Web
- V. Network Dynamics: Population Models
- VI. Network Dynamics: Structural Models
- VII. Institutions and Aggregate Behavior

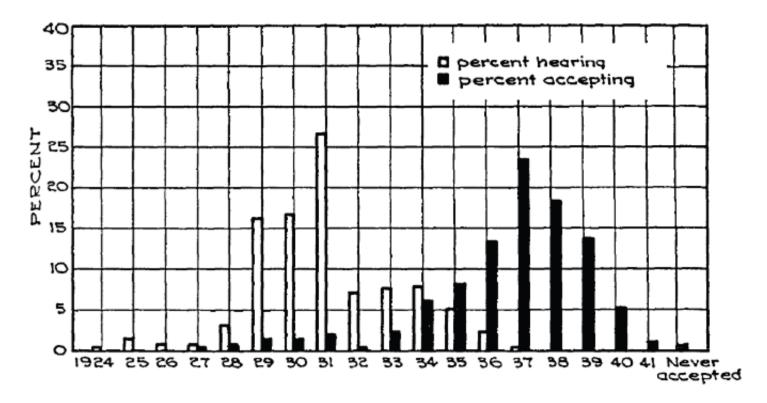
Graph Representation of a Network



Small World Phenomenon: The Watts-Strogatz model



The Power of Weak Ties



The years of first awareness and first adoption for hybrid seed corn in the Ryan-Gross study.

- I. Graph Theory and Social Networks
- II. Game Theory
  - □ Games
  - □ Evolutionary Game Theory
  - Modeling Network Traffic using Game Theory
  - Auctions
- III. Markets and Strategic Interaction in Networks
- IV. Information Networks and the World Wide Web
- V. Network Dynamics: Population Models
- VI. Network Dynamics: Structural Models
- VII. Institutions and Aggregate Behavior

The Prisoners' Dilemma

Game:

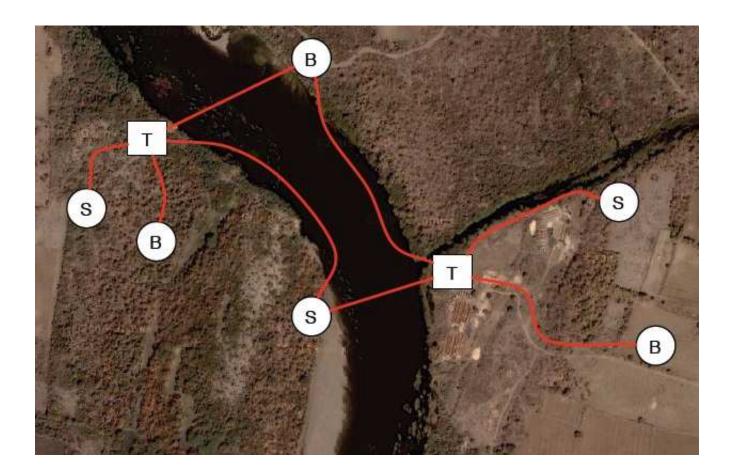
Should I use performance-enhancing drugs in professional sports or not?

Payoff matrix:

		Athlete 2	
		Don't Use Drugs	Use Drugs
Athlete 1	Don't Use Drugs	3,3	1, 4
	Use Drugs	4,1	2, 2

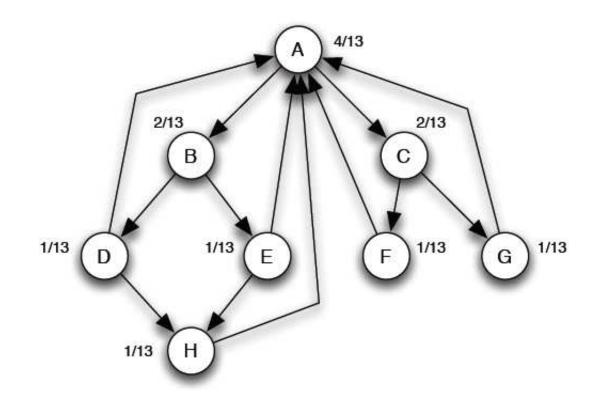
- I. Graph Theory and Social Networks
- II. Game Theory
- III. Markets and Strategic Interaction in Networks
  - Matching Markets
  - Network Models of Markets with Intermediaries
  - □ Bargaining and Power in Networks
- IV. Information Networks and the World Wide Web
- V. Network Dynamics: Population Models
- VI. Network Dynamics: Structural Models
- VII. Institutions and Aggregate Behavior

Markets and Trading



- I. Graph Theory and Social Networks
- II. Game Theory
- III. Markets and Strategic Interaction in Networks
- IV. Information Networks and the World Wide Web
  - □ The Structure of the Web
  - □ Link Analysis and Web Search
  - Sponsored Search Markets
- V. Network Dynamics: Population Models
- VI. Network Dynamics: Structural Models
- VII. Institutions and Aggregate Behavior

Link Analysis and Web Search



Equilibrium PageRank values for a network of eight web pages.

- I. Graph Theory and Social Networks
- II. Game Theory
- III. Markets and Strategic Interaction in Networks
- IV. Information Networks and the World Wide Web
- V. Network Dynamics: Population Models
  - Information Cascades
  - Network Effects
  - Power Laws and Rich-Get-Richer Phenomena
- VI. Network Dynamics: Structural Models
- VII. Institutions and Aggregate Behavior

Information Cascades and the Wisdom of the Crowd

Urns and Balls ...

The Wisdom of the Crowd

To maximize the chance of guessing correctly, you should guess majority-blue if

 $Pr[\text{ majority-blue } | \text{ what you have seen}] > \frac{1}{2}$ 

and guess *majority-red* otherwise.

Probabilities according to Bayes' Rule in the "Wisdom of the Crowd" szenario:

$$Pr[\text{ majority-blue } | \text{ blue}] = Pr[\text{ majority-red } | \text{ red}] = \frac{1/2 \times 2/3}{1/2} = \frac{2}{3}$$

Information Cascades

To maximize the chance of guessing correctly, you should guess majority-blue if

```
Pr[ majority-blue | what you have seen] > \frac{1}{2}
```

and guess *majority-red* otherwise. If the probability is exactly 0.5, it doesn't matter what you choose. Let's suppose you choose the color of your private signal, then.

Probabilities according to Bayes' Rule in the "Information Cascade" szenario:

**Person 1**  $Pr[majority-blue | blue] = Pr[majority-red | red] = \frac{1/2 \times 2/3}{1/2} = \frac{2}{3}$ **Person 2**  $Pr[majority-blue | blue, blue] > \frac{2}{3}$ 

... now an information cascade is going to start ...

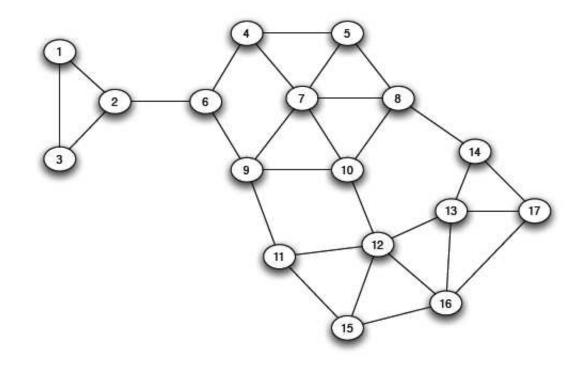
**Person 3**  $Pr[majority-blue | blue, blue, red] = \frac{4/27 \times 1/2}{1/9} = \frac{2}{3}$ All upcoming persons will reason just like Person 3.

#### Outline

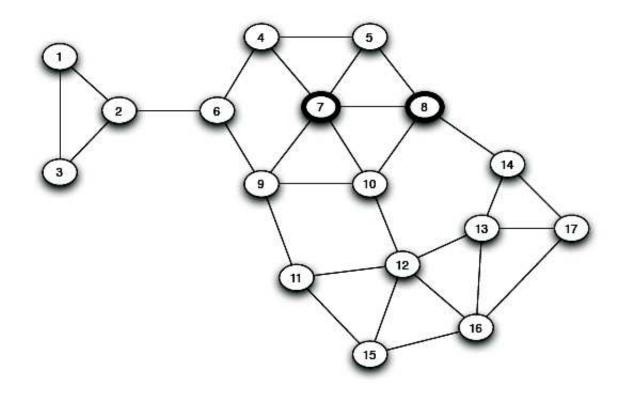
- I. Graph Theory and Social Networks
- II. Game Theory
- III. Markets and Strategic Interaction in Networks
- IV. Information Networks and the World Wide Web
- V. Network Dynamics: Population Models
- VI. Network Dynamics: Structural Models
  - Cascading Behavior in Networks
  - □ The Small-World Phenomenon
  - □ Epidemics

#### VII. Institutions and Aggregate Behavior

The Power of Strong Ties

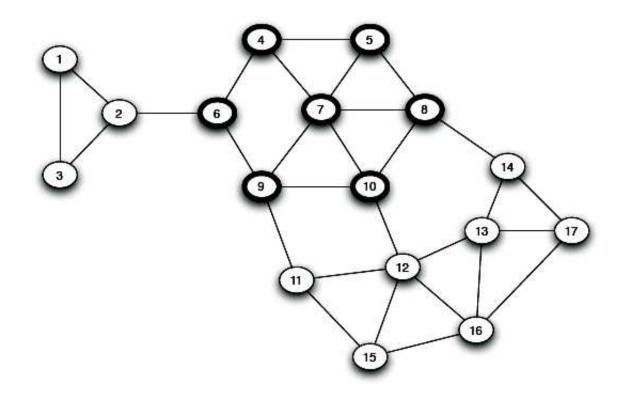


The Power of Strong Ties



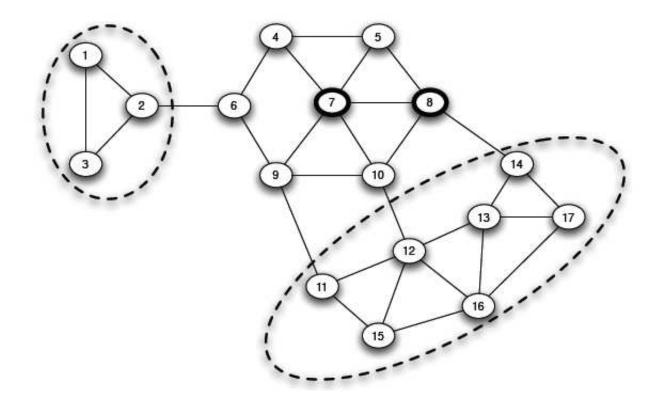
(a) Two nodes are the initial adopters

The Power of Strong Ties



(b) The process ends after three steps

The Power of Strong Ties



- I. Graph Theory and Social Networks
- II. Game Theory
- III. Markets and Strategic Interaction in Networks
- IV. Information Networks and the World Wide Web
- V. Network Dynamics: Population Models
- VI. Network Dynamics: Structural Models
- VII. Institutions and Aggregate Behavior
  - Markets and Information
  - □ Voting
  - Property Rights

**Covered Phenomena** 

- □ The Market for Lemons
- Arrows Impossibility Theorem
- □ The Tragedy of the Commons

Book freely available online!

END.