Clustering of Short Strings
TIR 2009 in L arge Databases
M. Kazimianec (FUB)
A. Mazeika (MPII)

## Outline

- Background (String Similarity, Proximity Graph (PG), GPC Method)
- Problem of Clustering Short Strings
- CLOSS. Milestones
- Border Identification
- Center Optimization
- PG Smoothing



## String Similarity

Each string is represented as a set (bag) of unordered q-grams;
One string is chosen as a counting point (center c);
Overlap O of the string s with the center c is computed;
Overlap O is accepted as a string similarity measure.
$c=$ string, $s_{1}=\operatorname{strip}, s_{2}=\operatorname{triad} ; q=2$.
$O\left(c, s_{1}\right)=\{\# s, s t, t r, r i, i n, n g, g \$\} \cap\{\# s, s t, t r, r i, i p, p \$\}=4$.
$O\left(c, s_{2}\right)=\{\# s, s t, t r, r i, i n, n g, g \$\} \cap\{\# t, t r, r i, i a, a d, d \$\}=2$.
"strip" is more similar to "string" than "triad".

## Proximity Graph

Proximity graph (PG) is a discrete numerical decreasing function depending on overlap threshold expressed by the integer value $i$.
In the point $\mathrm{i} P G$ value is a number of strings that have overlap O with the center c not exceeding the given threshold i.


## GPC M ethod for String Clustering

GPC takes a center string and examines the shape of the proximity graph. If there is a horizontal line (overlaps $3,4,5$ ) then GPC declares the cluster border in the extreme right point of the line (border $=5$, cluster $=$ \{malcolm, malcom, makolm $\}$ ).


## W hat A re the GPC Disadvantages?

GPC is weak if:

- horizontal line is not present in the PG (short strings),
- there are multiple horizontal lines in the PG (long and middle strings),
- dataset is not ordered by string length.

GPC application is cut down by following PG model:


## Problems of Clustering Short Strings

- Touching Clusters - PG has no horizontal lines,
- Overlapping Clusters - PG has multiple horizontal lines.



## Border Identification

## Oxford D ataset Sample

|  | String | qlength | sborder | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | countenance | 12 | 8 | 12 | 8 | 10 | 6 | 5 | 6 | 6 | 6 | 6 | 5 | 5 | 6 | 5 | 3 | 6 |
| 2 | contanance | 11 | 8 | 8 | 11 | 9 | 6 | 6 | 6 | 6 | 6 | 6 | 6 | 6 | 6 | 6 | 4 | 4 |
| 3 | contenance | 11 | 9 | 10 | 9 | 11 | 6 | 7 | 7 | 7 | 7 | 7 | 7 | 7 | 7 | 7 | 4 | 7 |
| 4 | conscience | 11 | 6 | 6 | 6 | 7 | 11 | 6 | 7 | 7 | 8 | 8 | 8 | 7 | 8 | 7 | 4 | 6 |
| 5 | conceince | 10 | 6 | 5 | 6 | 6 | 6 | 10 | 7 | 6 | 6 | 6 | 6 | 8 | 5 | 6 | 3 | 6 |
| 6 | conciance | 10 | 7 | 6 | 7 | 7 | 7 | 7 | 10 | 7 | 6 | 6 | 6 | 7 | 6 | 6 | 4 | 6 |
| 7 | convenience | 12 | 9 | 6 | 6 | 7 | 7 | 8 | 6 | 12 | 9 | 11 | 7 | 7 | 7 | 8 | 5 | 9 |
| 8 | convience | 10 | 9 | 6 | 6 | 7 | 8 | 6 | 6 | 9 | 10 | 10 | 6 | 7 | 6 | 6 | 4 | 6 |
| 9 | convienience | 13 | 10 | 6 | 6 | 7 | 8 | 6 | 6 | 11 | 10 | 13 | 7 | 7 | 7 | 8 | 5 | 9 |
| 10 | consequence | 12 | 10 | 6 | 6 | 7 | 8 | 6 | 6 | 7 | 7 | 7 | 12 | 10 | 10 | 7 | 4 | 7 |
| 11 | concequence | 12 | 9 | 6 | 6 | 7 | 7 | 8 | 7 | 7 | 6 | 7 | 10 | 12 | 9 | 7 | 4 | 7 |
| 12 | consiquence | 12 | 9 | 6 | 6 | 7 | 8 | 6 | 6 | 7 | 7 | 7 | 10 | 9 | 12 | 7 | 4 | 7 |
| 13 | convalescence | 14 | 8 | 6 | 6 | 7 | 8 | 7 | 6 | 8 | 8 | 7 | 7 | 7 | 7 | 14 | 8 | 11 |
| 14 | convalaces | 11 | 7 | 3 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 8 | 11 | 7. |
| 15 | convalensence | 14 | 7 | 6 | 6 | 7 | 7 | 6 | 6 | 7 | 7 | 8 | 8 | 7 | 7 | 11 | $7{ }^{\circ}$ | 14 |

Blue color marks out subjective (true) clusters. Red color shows alien strings for SH border. The last is minimal overlap preserving all misspellings.

## How we solve...

The task is to minimize the number of alien strings in the cluster maximally preserving misspellings.

The solution is related to the CLOSS method (Clustering of Short Strings)
$\square$ Center optimization (by string ordering)

- Border identification
- Resolving of multiple PG lines


## CLOSS. Dataset Ordering

The choice of the shorter center may lead to a PG shape without horizontal line even for long strings:


Center is malcolm


Center is malcom

Ordering by string length and clustering starting from the longest strings resolve this problem.

## CLOSS. B order Interval

Border interval $\left[i^{1}, i^{1}\right]$ is found by means of PG interpolation by the polynomial $f(x)$.
Starting point $i^{\prime}$ is set to the overlap value, where the curvature of $f(x)$ is maximal":

$$
i^{\prime}=\arg \max _{i}\left\{\frac{\left|f^{(2)}(i)\right|}{\left[1+\left(f^{(1)}(i)\right)^{2} \frac{3}{2}^{\frac{3}{2}}\right.}\right\} .
$$

Ending point $\mathrm{i}^{\prime \prime}$ is set to be $k \cdot q$ numbers of $q$-grams away from the
 maximal overlap

$$
\mathrm{i}^{\prime \prime}=\text { length }(\mathrm{s})+\mathrm{q}(1-\mathrm{k})-1 .
$$

## CLOSS. Border Point

Let $\left[i^{\prime}, i^{\prime \prime}\right]$ be the border interval. Then $i_{b} \in\left[i^{\prime}, i^{\prime \prime}\right]$ is the cluster border iff
(i) $i_{b}=\arg \min _{i}\left\{\Delta_{i}(s), i=i^{\prime}, i^{\prime}+1, \ldots, i^{\prime \prime}\right\}$, where $\Delta_{i}(s)=$
$=N_{i}(s)-N_{i+1}(s) \geq 0$ is the PG neighborhood decrease at the overlap threshold $i$;
(ii) $\nexists j<i_{b}, j \in\left[i^{\prime}, i^{\prime}\right]: \Delta_{j}(s)=\Delta_{i_{b}}(s)$.

Defined border exists independently of the PG shape.

## Algorithm

```
Input:
    D = {s, , s, ,\ldots, sn}: database of ordered strings,
    q: size of q-grams, r: range of smoothing.
Output:
    Clusters }={\mp@subsup{C}{1}{},\ldots,\mp@subsup{C}{d}{}}: clusters of strings
Body:
    1. Initialize the clustered strings
    Clustered_Strings = \emptyset; Clusters ={\emptyset}.
    2. Scan database strings. For each s}\inD D
        2.1. If s & Clustered_Strings Then
            2.1.1. Compute the proximity graph
        PG(s)={(1,N N (s)),\ldots,(l,N泣(s))} (see [1]).
            2.1.2. Compute the smoothed proximity graph
                PG}\mp@subsup{}{}{sm}(s)=Smooth(PG(s),1,l,r) (see Figure 5)
            2.1.3. Find the interval [ [ }\mp@subsup{i}{}{\prime},\mp@subsup{i}{}{\prime\prime}
            2.1.4. Find the border ib}\inP\mp@subsup{i}{}{am}(s),\mp@subsup{i}{b}{}\in[\mp@subsup{i}{}{\prime},\mp@subsup{i}{}{\prime\prime}]\mathrm{ ,
                by computing the PG jump }\mp@subsup{\Delta}{\mp@subsup{i}{b}{}}{sm}(s)
                \mp@subsup{\Delta}{ib}{sm}}(s)=\mp@subsup{\operatorname{min}}{i}{}{\mp@subsup{\Delta}{i}{sm}(s)}\mathrm{ , where
                \mp@subsup{\Delta}{i}{sm}}(s)=\mp@subsup{N}{i}{sm}(s)-\mp@subsup{N}{i+1}{sm}(s)
            2.2 Update the clustered strings:
            Clustered_Strings = Clustered_Strings }\cup\mp@subsup{C}{\mp@subsup{i}{b}{}}{}\mathrm{ ,
            Cib
        2.4 Insert a new cluster to the set of clusters:
            Clusters = Clusters }\cup{\mp@subsup{C}{\mp@subsup{i}{b}{}}{}}
3. Return Clusters.
```


## Evaluation. Clustering of the Cyclone Name Dataset

CLOSS and GPC (improved by string ordering) were compared by applying them to the cyclone name dataset (www.nhc.noaa.gov/aboutnames.html) artificially corrupted by introducing
one mistake

many (up to 3) mistakes


## Evaluation. Text Retrieval Using Oxford M isspellings

CLOSS was used to enhance text retrieval by means of misspellings. File "birkbeck" (http://ota.ahds.ac.uk/), containing 36133 misspellings of 6136 words, was considered as a misspelling source.


PG Shapes

$\Delta_{\mathrm{CLOSs} / \mathrm{GPC}}=1-\frac{\mathrm{C}^{\text {corr }}}{\mathrm{C}}$

## CLOSS and Subjective Clustering

|  |  |  | Overlap number |  |  |  |  |  |  |  |  |  |  |  |  |  | CLOSS Border |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| String | qlength | border | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | CLOSS1 | CLOSS2 |
| countenance | 12 | 8 | 15 | 15 | 15 | 14 | 14 | 10 | 10 | 3 | 2 | 2 | 1 | 1 | 0 | 0 | 4 | 9 |
| contanance | 11 | 8 | 15 | 15 | 15 | 15 | 13 | 13 | 3 | 3 | 2 | 1 | 1 | 0 | 0 | 0 | 5 | 7 |
| contenance | 11 | 9 | 15 | 15 | 15 | 15 | 14 | 14 | 13 | 3 | 3 | 2 | 1 | 0 | 0 | 0 | 5 | 8 |
| conscience | 11 | 6 | 15 | 15 | 15 | 15 | 14 | 14 | 9 | 5 | 1 | 1 | 1 | 0 | 0 | 0 | 5 | 9 |
| conceince | 10 | 6 | 15 | 15 | 15 | 14 | 14 | 12 | 3 | 2 | 1 | 1 | 0 | 0 | 0 | 0 | 4 | 4 |
| conciance | 10 | 7 | 15 | 15 | 15 | 15 | 14 | 14 | 7 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 5 | 8 |
| convenience | 12 | 9 | 15 | 15 | 15 | 15 | 15 | 14 | 11 | 6 | 4 | 2 | 2 | 1 | 0 | 0 | 10 | 10 |
| convience | 10 | 9 | 15 | 15 | 15 | 15 | 14 | 14 | 6 | 4 | 3 | 2 | 0 | 0 | 0 | 0 | 5 | 5 |
| convienience | 13 | 10 | 15 | 15 | 15 | 15 | 15 | 14 | 10 | 6 | 4 | 3 | 2 | 1 | 1 | 0 | 9 | 11 |
| consequence | 12 | 10 | 15 | 15 | 15 | 15 | 14 | 14 | 10 | 4 | 3 | 3 | 1 | 1 | 0 | 0 | 5 | 9 |
| concequence | 12 | 9 | 15 | 15 | 15 | 15 | 14 | 14 | 11 | 4 | 3 | 2 | 1 | 1 | 0 | 0 | 5 | 5 |
| consiquence | 12 | 9 | 15 | 15 | 15 | 15 | 14 | 14 | 10 | 4 | 3 | 2 | 1 | 1 | 0 | 0 | 5 | 5 |
| convalescence | 14 | 8 | 15 | 15 | 15 | 15 | 15 | 15 | 12 | 6 | 2 | 2 | 2 | 1 | 1 | 1 | 9 | -20 |
| convalaces | 11 | 7 | 15 | 15 | 15 | 14 | 3 | 3 | 3 | 2 | 1 | 1 | 1 | 0 | 0 | 0 | 5 | . 9 |
| convalensence | 14 | 7 | 15 | 15 | 15 | 15 | 15 | 15 | 11 | 4 | 2 | 2 | 2 | 1 | 1 | 1 | 8 | IS9 |

## CLOSS and Subjective Clustering

Preserving misspellings CLOSS reduces the number of alien strings.


## M ultiple Horizontal Lines Problem

Typical example is the DBLP dataset of paper titles.


Multiple horizontal lines arise because of the common words (and their parts) in the titles.

## CLOSS. Smoothing

Smoothing modifies the PG shape by using moving averages. This allows to identify cluster border for the case of multiple lines that take place in datasets containing long and short/long strings.

$$
N_{i}^{s m}(s)=\frac{1}{2 r+1} \sum_{j=i-r}^{i+r} N_{j}(s)
$$



PG without smoothing


Smoothed PG

## Resume

- Proposed method is intended to cluster strings in textual databases of different origin. It uses dataset ordering, string representation by q-grams, novel border identification technique as well as proximity graph smoothing (for the case of multiple horizontal lines).
- Evaluation shows CLOSS efficiency for datasets with strings of different length, even if cluster border is not prominent (short strings).


## Future Investigations

- It is observed that if PG has multiple horizontal lines then clustering quality varies depending on string length and smoothing interval. In the nearest future we suppose to stabilize the quality applying adaptive smoothing that takes into account string length dispersion in each point of the proximity graph.


## Questions

$?$

